

DEPARTMENT OF MATHEMATICS

**COURSE OUTLINE TEMPLATE**

Course Title	<b>Mathematics – II</b>		
Course Code	<b>MAIR21</b>	No. of Credits : <b>4 (3L + 1T)</b>	
Department	<b>Mathematics</b>	Section: <b>ICE A &amp; B</b>	
Pre-requisites Course Code	<b>MAIR11-Mathematics-I</b>		
Course Teacher(s)/Tutor(s)	Email Id	Telephone No.	
<b>Dr. V. Shanthi</b>	<b>vshanthi@nitt.edu</b>	<b>9487440341</b>	
Course Type	<b>Core course</b>		

**COURSE OVERVIEW**

- This course will introduce basic structures of linear algebra (i.e., vector space and inner product space).
- This course will familiarize theory and application of functions of complex variable and vector valued functions.
- This course will introduce theory and application of higher order differential equations.

**COURSE OBJECTIVES**

**Learning Objectives:** Objective of the course is to

1. Introduce the structure vector space and various operations on it.
2. Introduce different method to solve the 2<sup>nd</sup> order differential equations and its applications in electric circuit problems.
3. familiarize concepts like differentiations and integration for function of complex variable.
4. Introduce vector differential operator for vector function and important theorems on vector functions to solve engineering problems.

**COURSE OUTCOMES (CO)**

Course Outcomes	Aligned Programme Outcomes(PO)
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After the completion of the course, students would be able to

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- Perform standard operation in finite dimensional vector spaces
- Compute the dot product of vectors, lengths of vectors, and angles between vectors.
- Perform gradient, div, curl operator on vector functions and give physical interpretations.
- Use Green's , Gauss divergence and Stoke's theorems to solve engineering problems.
- solve higher order ODEs and interpret it geometrically.
- Compute differentiation of functions of complex variable.
- Construct analytic function for given real or imaginary part of it.
- find images of the given region by standard functions of complex variable.
- compute bilinear map by knowing the images of three points.

## MAIR21 MATHEMATICS- II

Vector space – Subspaces – Linear dependence and independence – Spanning of a subspace – Basis and Dimension. Inner product – Inner product spaces – Orthogonal and orthonormal basis – Gram- Schmidt orthogonalization process.

Basic review of first order differential equation - Higher order linear differential equations with constant coefficients –Particular integrals for  $x^n, e^{ax}, e^{ax} \cos(bx), e^{ax} \sin(bx)$  – Equation reducible to linear equations with constant coefficients using  $x = e^t$  - Simultaneous linear equations with constant coefficients – Method of variation of parameters – Applications – Electric circuit problems.

Gradient, Divergence and Curl – Directional Derivative – Tangent Plane and normal to surfaces – Angle between surfaces –Solenoidal and irrotational fields – Line, surface and volume integrals – Green's Theorem, Stokes' Theorem and Gauss Divergence Theorem (all without proof) – Verification and applications of these theorems.

Analytic functions – Cauchy – Riemann equations (Cartesian and polar) –Properties of analytic functions – Construction of analytic functions given real or imaginary part – Conformal mapping of standard elementary functions ( $Z^2, e^z, \sin z, \cos z, z + \frac{k^2}{z}$ ) and bilinear transformation.

Cauchy's integral theorem, Cauchy's integral formula and for derivatives– Taylor's and Laurent's expansions (without proof) – Singularities – Residues – Cauchy's residue theorem – Contour integration involving unit circle.

## COURSE TEACHING AND LEARNING ACTIVITIES

S.No.	Week	Topic	Mode of Delivery
	Week 1 & 2	Introduction of D.E, First order differential equation and its solution, Higher order homogeneous Linear differential Equations and its soln. Particular integrals of various Types. Simultaneous Differential Equations, Method of Variation of Parameters, Applications – Electric Circuit Problems.	Chalk and Talk
	Week 3 & 4  Week 5	Introduction to Vector spaces and examples of VS, Subspaces and examples, Linear independence, linear dependence, Span, Basis, Dimension, Inner Product spaces & Orthogonality, Ortho normal basis, Gram Schmidt orthogonalization process.  <b>Assessment –I</b>  Topics covered in first 4 weeks.	Chalk and Talk
	Week 5 & 6  Week 7 & 8  Week 9	Introduction to function complex variable and analyticity of complex function. Geometrical properties of complex function. Some standard conformal maps  Integral of complex function and the important theorems on complex function for closed contour integration. Taylor & Laurent's series for complex functions.  <b>Assessment –II</b>  Topics covered in 5 <sup>th</sup> to 8 <sup>th</sup> weeks.	Chalk and Talk

	<b>Week 9 &amp; 10</b>	Introduction to vector valued function and different operator (grad, del, div) for vector valued function. Important theorems (Green's theorem, Gauss divergence and Stoke's theorem) on vector valued function which connects line, double & triple integral of vector valued function.	
	<b>Week 11 &amp; 12</b>	<b>Semester examination (portion: all the topics)</b>	

#### COURSE ASSESSMENT METHODS

S.No		Week/Date	Duration	% Weightage
1.	Assessment t -I	6 <sup>th</sup> Week	1 Hour	20%
2.	Assessment-II	12 <sup>th</sup> Week	1 Hour	20%
3.	Reassessment for Assessment I & II	13 <sup>th</sup> Week	1 Hour	20%( Assessment I & II portions )
4.	Assessment -III (Assignment)	5 <sup>th</sup> week & 13 <sup>th</sup> week		(5 + 5 = 10%)
5.	Final Assessment		3 Hours	50% Total : 100 Marks

**ESSENTIAL READINGS : Textbooks, reference books Website addresses, journals, etc**

**Reference Books:**

1. Kreyszig.E , Advanced Engineering Mathematics, 10<sup>th</sup> edition, John Wiley Sons, 2010
2. Grewal,B.S., Higher Engineering Mathematics, 43<sup>rd</sup> edition, Khanna Publications, Delhi.
3. Gilbert Strang, Linear Algebra and its applications, 4<sup>th</sup> edn, Cengage Learning, 2006.
4. James Ward Brown and Ruel V. Churchill, Complex and Applications, 9<sup>th</sup> edn, McGraw-Hill, 2013.

**COURSE EXIT SURVEY (mention the ways in which the feedback about the course is assessed and indicate the attainment also)**

1. Students can meet the faculty at any stage in the course duration in case he/she finds difficulty in understanding the concept.
2. Feedback form issued to students to express their comments about the course before cycle test 1 & after completing the syllabus. Students are requested to give genuine feedback about the course.
3. Student knowledge about the topic covered in this course will be judged through marks obtained in examination.

**COURSE POLICY (including plagiarism, academic honesty, attendance, etc.)**

**1. Examination:**

- a) Students who have missed the first or second cycle test or both can register for Re-Test examination which shall be conducted soon after the completion of the second cycle test and before the regular semester examination.
- b) The Re-Test examination shall be conducted for 20 marks comprising the syllabus of both first and second cycle tests.
- c) Students should submit assignments before last date of submission. In case students fails to submit their assignments, he/she will get zero mark for that particular assignment.

**2. Attendance:**

- a) The minimum attendance for appearing for the semester examination is 75%.
- b) Those students, whose attendance falls below 75% but above 50% in a subject, shall attend mandatory classes before the semester examinations to qualify to

write semester exam.

- c) The students who are having attendance less than or equal to 50% has to redo the course.

3. The Institute follows relative grading with flexibility given to teachers to decide the mark ranges for grades. All assessment of a course will be done on the basis of marks.
4. The passing minimum should be  $\frac{\bar{X}}{2}$  or  $X_{max}/3$ , whichever is less Where  $\bar{X}$  is the mean of the class and  $X_{max}$  is the maximum mark in the class.
5. The Performance Analysis Committee, which shall meet within couple of weeks after the completion of all examinations, shall analyze the relative cumulative performance of students in all examinations (continuous and end-semester) of a course and finalize the letter grade ranges for the course.
6. The letter grades and the corresponding grade points are as follows:

<b>Letter</b>	<b>S</b>	<b>A</b>	<b>B</b>	<b>C</b>	<b>D</b>	<b>E,R</b>	<b>F,I</b>	<b>V</b>	<b>FF</b>	<b>X</b>
<b>Grade(GP)</b>	<b>10</b>	<b>9</b>	<b>8</b>	<b>7</b>	<b>6</b>	<b>5</b>	<b>0</b>	<b>-</b>	<b>2</b>	<b>-</b>

- a) Students scoring less than the passing minimum marks in the assessments defined in the course plan shall be deemed to have not successfully completed the course and be given an 'F' grade.
- b) Students awarded F grade may REDO the course or opt for formative assessment.
- c) 'V' indicates lack of required attendance. Students awarded 'V' grade must compulsorily redo the course.
- d) 'I' grade indicates incompleteness of formative assessment.
- e) A student who gets an 'I' grade must necessarily convert it to a 'R' grade by completing the formative assessment.
- f) An 'FF' grade is awarded for not completing the formative assessment in the prescribed maximum period of study due to gross negligence. An 'FF' grade will have a grade point of 2 and it will remain on the grade card permanently. This will be used in the CGPA calculations.
- g) A student who earns a minimum of 5 grade points (a 'E' grade or a 'R' grade) in a course is declared to have successfully completed the course.
- h) If the students fails to appear semester examination due to genuine/medical reason, can register for special end semester examination after approval from course teacher & Head of department of Mathematics/Dean(academic). The special end semester examination will be conducted within ten days from reopening of institute for next semester.**


Students should register their names with course teacher to appear for special end semester examination within three days from reopening of institute for next semester. Grade issued as per the guidelines followed for his/her batch students.

- i) There will be one reassessment (for 90 marks) for the students who have secured "F" in this course and will be conducted within ten days from reopening of institute for next semester. Students should register their names with course teacher to appear for reassessment within three days from reopening of institute for next semester. If the students satisfy the criteria fixed by the faculty to promote E grade will be given E grade and others given 'F' grade.


#### ADDITIONAL COURSE INFORMATION

Students can reach course faculty by fixing appointment through E-mail (vshanthi@nitt.edu or phone [9487440341 or intercom: 3673, during office hours (8.30am-5.15pm)].

#### FOR SENATE'S CONSIDERATION

  
Dr. V. SHANTHI  
(Course Faculty)

  
CC-Chairperson

  
Dr. K. Murugesan, Professor  
Head, Dept. of Maths

10/11/2017  
**Dr. K. MURUGESAN**  
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